

# iUML-B

# State Machine Diagrams

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# Motivation

Provide a more approachable interface for newcomers to Event-B

Provide diagrams to help visualise models

Provide extra modelling features to Event-B

- Sequencing of Events

- Lifting of Behaviour to a set of instances (O-O)

N.b. not trying to formalise UML

# What is iUML-B?

A Graphical front-end for Event-B

- ▶ Plug-in for Rodin

Not UML ...

- ▶ Has its own meta-model (abstract syntax)
- ▶ Semantics inherited from translation to Event-B

... but it has some similarities with UML

- ▶ Class Diagrams *Coming soon!*
- ▶ State Machine Diagrams

Translator generates Event-B automatically

- ▶ Into the same machine (generated is read only)
- ▶ Can also write standard Event-B in the same machine + events

# What are the benefits?

## Visualisation

- ▶ Helps understanding
- ▶ communication

## Faster modelling

- ▶ One drawing node = several lines of B
- ▶ Extra information inferred from position (containment) of elements
- ▶ Experiment with different abstractions

*finding useful abstractions is hard*

## Provides structuring constructs

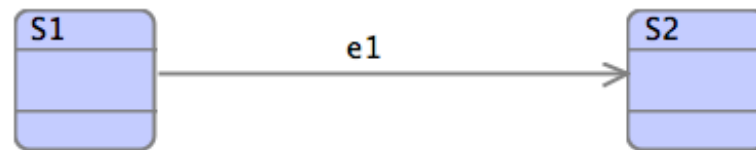
- ▶ Hierarchical state-machines  
Event-B has no *event sequencing* mechanism
- ▶ Class Lifted state-machines  
Event-B has no *lifting* mechanism

# State Machines

State machines provide a way to model behaviour (transitions)

Constrained by some data (source state)

The transition's behaviour is to change the data (to target state)

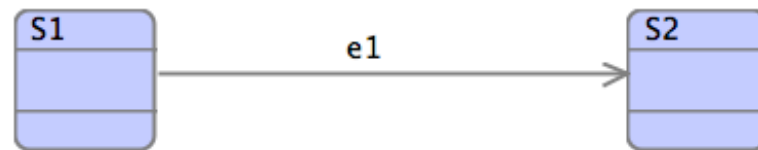


Transition **e1** can only fire when the state is **S1**

when **e1** fires it changes the state to **S2**

*How could we represent this in Event-B?*

# State Machines to Events



## EVENTS

$e1 \triangleq$  WHEN *<in S1>* THEN *<becomes S2>* END

where, *<in S1>* and *<becomes S2>* depend on the data that represents state

# State machine as a type

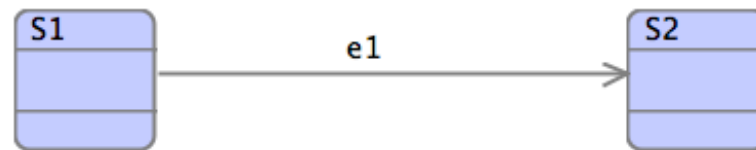
We could treat the whole statemachine as an enumerated type. The current state is given by a variable of that type. (Called **Enumeration** translation in iUML-B).

## VARIABLES

$sm \in sm\_STATES$

## SETS

$sm\_STATES = \{S1, S2\}$



## EVENTS

$e1 \triangleq \text{WHEN } sm = S1 \text{ THEN } sm := S2 \text{ END}$

# State machine collection of variables

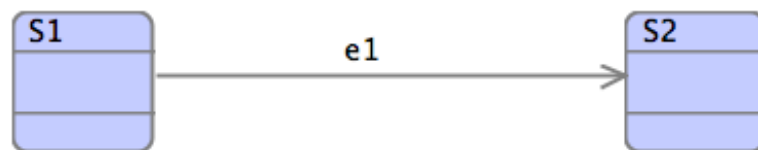
Or we could treat each state as a separate variable. (Called **Variables** translation in iUML-B)

## VARIABLES

**S1** ∈ B00L

**S2** ∈ B00L

*where, one of S1, S2 is TRUE at any moment*

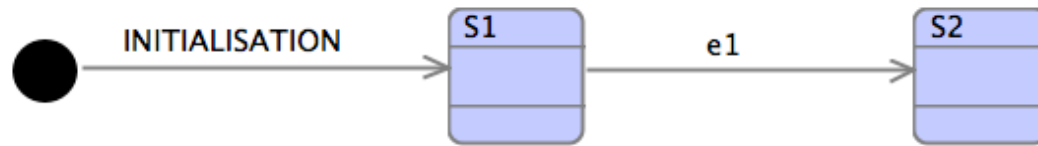


## EVENTS

```
e1 ≙ WHEN S1 = TRUE
      THEN S1 := FALSE
           S2 := TRUE
      END
```



# Initial transition



Enumeration translation

INITIALISATION

$sm := S1$

or

Variables translation

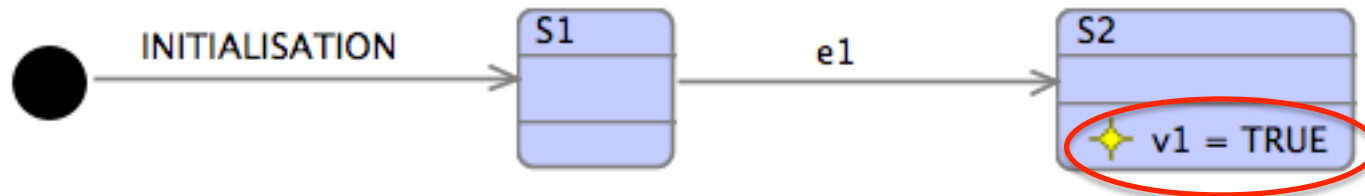
INITIALISATION

$S1 := TRUE$

$S2 := FALSE$

# State Invariant

Something that must be true whenever the system is in that state.



Enumeration translation

INVARIANTS

$(sm=S2) \Rightarrow (v1=TRUE)$

or

Variables translation

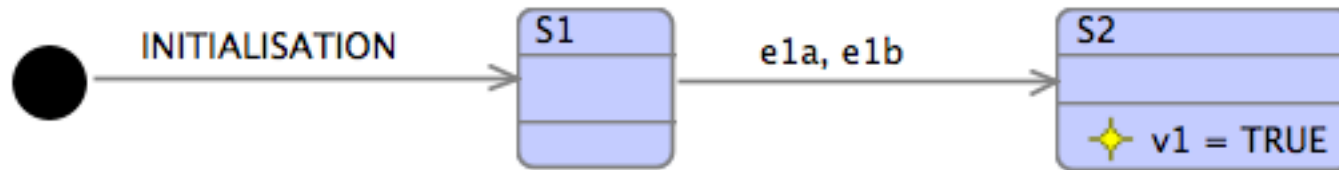
INVARIANTS

$(S2=TRUE) \Rightarrow (v1=TRUE)$

# Transition Elaboration

Transitions 'elaborate' (i.e. contribute to) event(s) in the Machine.

So you can give them parameters, guards and actions etc. in the Machine



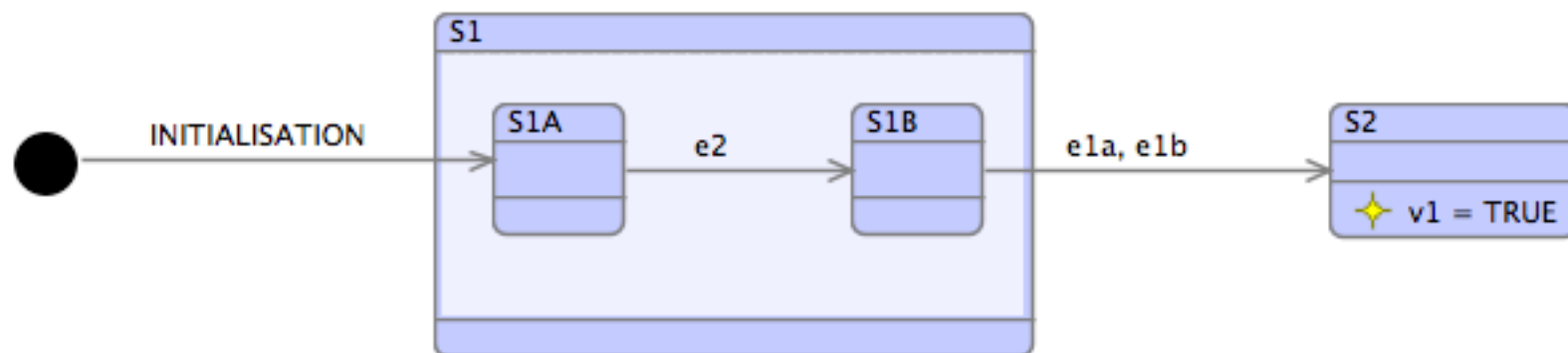
```
e1a ≐  
STATUS  
ordinary  
ANY  
p  
WHERE  
isin_S1 : S1 = TRUE  
grd1 : p > 5  
THEN  
leave_S1 : S1 = FALSE  
enter_S2 : S2 = TRUE  
END
```

```
e1b ≐  
STATUS  
ordinary  
ANY  
p  
WHERE  
isin_S1 : S1 = TRUE  
grd1 : p ≤ 5  
THEN  
enter_S2 : S2 = TRUE  
leave_S1 : S1 = FALSE  
END
```

# Nested State-machines

State-machines can be nested inside states

- a) so that we can put an invariant on the superstate
- b) so that a transition can leave from any substate
- c) adding detail in a refinement



## REFINEMENT of State-machines:

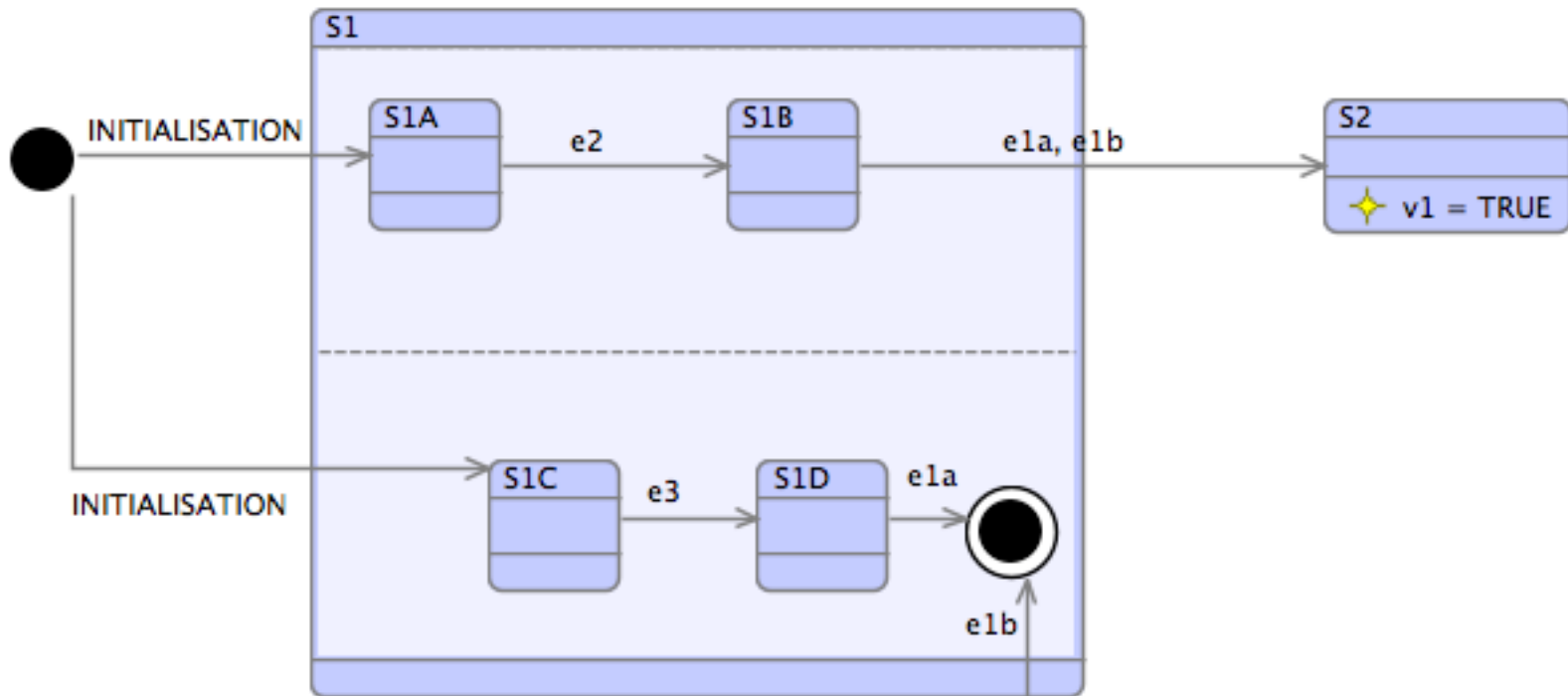
We often add nested state-machines in refinements.

Can also split events into cases (e.g. e1 to e1a,e1b) and add invariants to states

BUT must NOT add states to an existing state-machine as this would break the type/partition invariants.

# Parallel Nested State Machines

Several State machines can be nested inside states



# Transition Properties

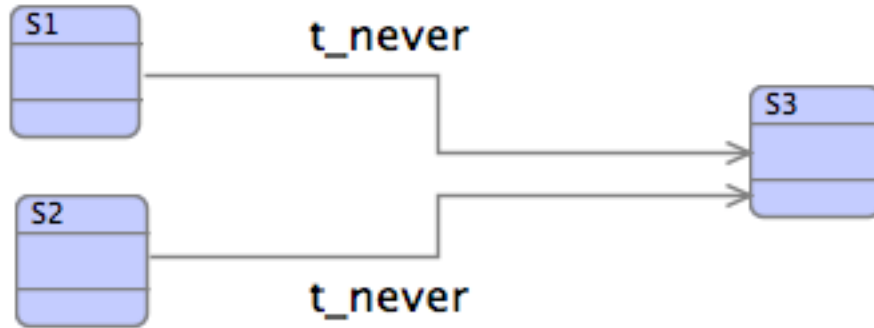
Transitions can own event properties:  
parameters, witnesses, guards and actions

Transition properties are copied into each elaborated event when the statemachine is generated.

Why? :

- a. You can do all the modelling in the diagram, no need to switch to the Event-B editor
- b. If several events are elaborated you only write the guards/actions etc. once

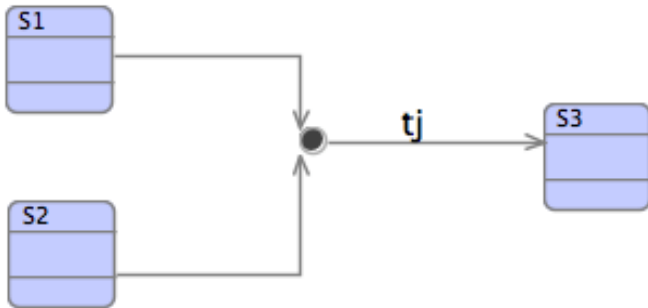
# Warning: Make sure transitions are possible!!



- o `t_never:` not extended ordinary >  
WHERE
  - o `isin_S2:` `S2 = TRUE` not theorem >
  - o `isin_S1:` `S1 = TRUE` not theorem >THEN
  - o `leave_S2:` `S2 = FALSE` >
  - o `leave_S1:` `S1 = FALSE` >
  - o `enter_S3:` `S3 = TRUE` >END

# Junctions

For transitions that are enabled in several states



- o `tj`: not extended ordinary >  
WHERE  
o `isin_S1_or_isin_S2`:  $(S1 = TRUE \vee S2 = TRUE)$   
THEN  
o `leave_S2`: `S2 = FALSE` >  
o `leave_S1`: `S1 = FALSE` >  
o `enter_S3`: `S3 = TRUE` >  
END

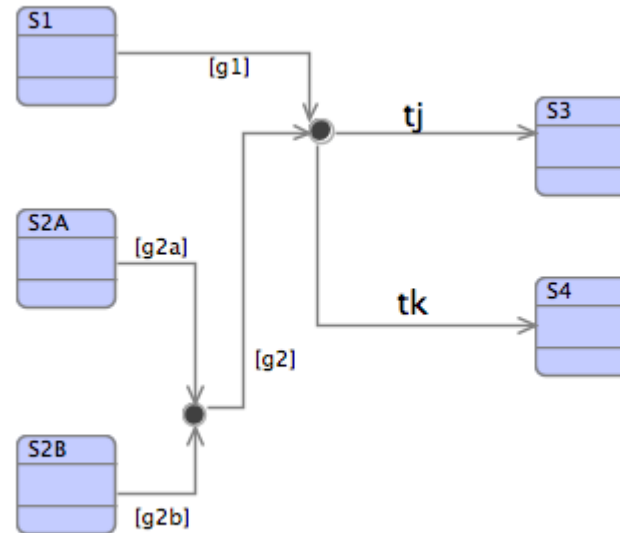
Rules:

1. Only the final segment elaborates an event
2. Other segments do not own actions (but can have guards)



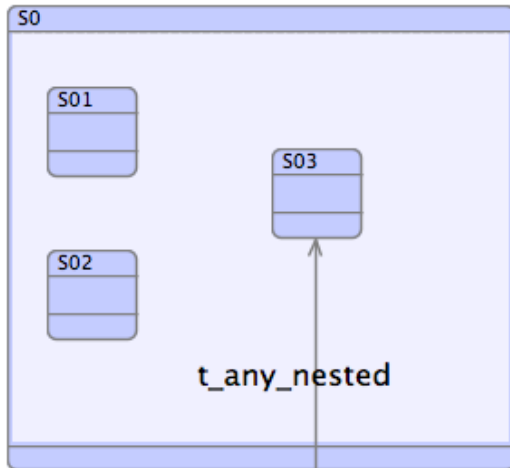
# Junctions (cont.)

Can be combined



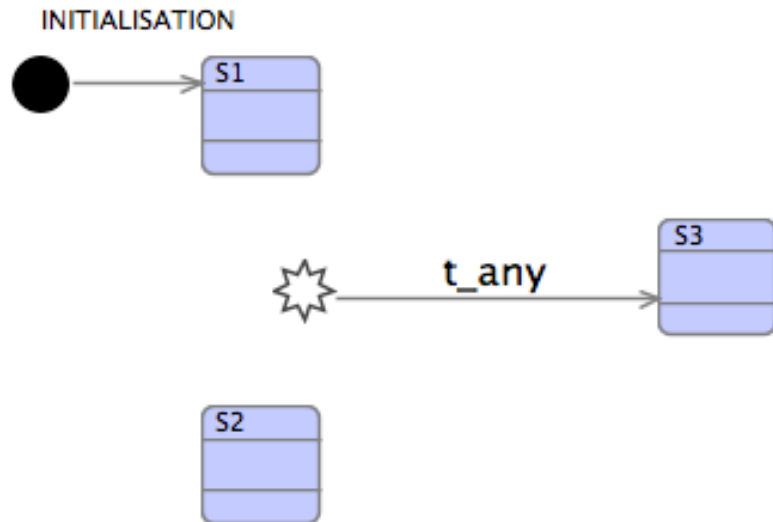
- o **tj**: not extended ordinary >  
WHERE  
o  $\text{isin\_S1\_or\_isin\_S2A\_or\_isin\_S2B: } ((S1 = \text{TRUE} \wedge \underline{g1}) \vee (((S2A = \text{TRUE} \wedge g2a) \vee (S2B = \text{TRUE} \wedge g2b)) \wedge g2))$   
THEN  
o leave\_S2B: S2B = FALSE >  
o leave\_S2A: S2A = FALSE >  
o leave\_S1: S1 = FALSE >  
o enter\_S3: S3 = TRUE >  
END
- o **tk**: not extended ordinary >  
WHERE  
o  $\text{isin\_S1\_or\_isin\_S2A\_or\_isin\_S2B: } ((S1 = \text{TRUE} \wedge \underline{g1}) \vee (((S2A = \text{TRUE} \wedge g2a) \vee (S2B = \text{TRUE} \wedge g2b)) \wedge g2))$   
-----

# From any substate



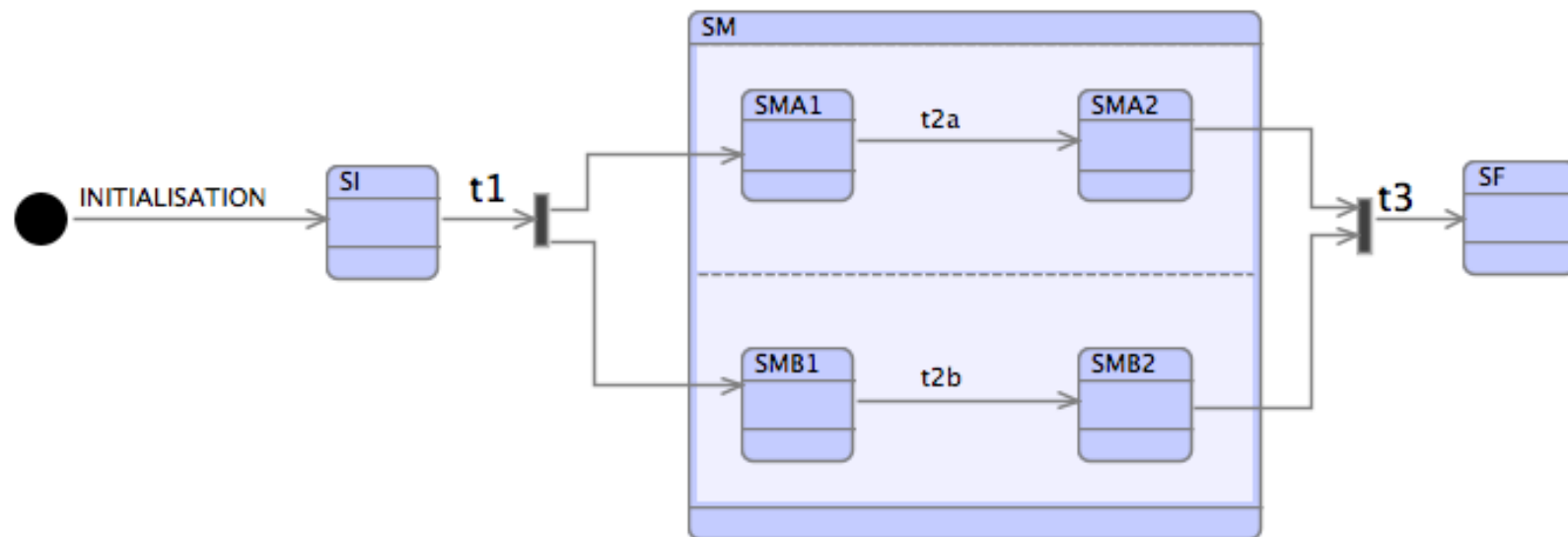
- o `t_any_nested:` not extended ordinary >  
WHERE
- o `isin_S0:` `S0 = TRUE` not theorem >  
THEN
- o `leave_S02:` `S02 = FALSE` >
- o `leave_S01:` `S01 = FALSE` >
- o `enter_S03:` `S03 = TRUE` >  
END

# From ANY at top level



- o `t_any`: not extended ordinary >  
THEN
  - o `leave_S2`: `S2 = FALSE` >
  - o `leave_S1`: `S1 = FALSE` >
  - o `enter_S3`: `S3 = TRUE` >END

# Forks and Joins



- o **t1:** not extended ordinary >  
**WHERE**
  - o isin\_SI: SI = TRUE not theorem >**THEN**
  - o leave\_SI: SI = FALSE >
  - o enter\_SMB1: SMB1 = TRUE >
  - o enter\_SM: SM = TRUE >
  - o enter\_SMA1: SMA1 = TRUE >**END**

- o **t3:** not extended ordinary >  
**WHERE**
  - o isin\_SMA2: SMA2 = TRUE not theorem >
  - o isin\_SMB2: SMB2 = TRUE not theorem >**THEN**
  - o leave\_SMA2: SMA2 = FALSE >
  - o leave\_SM: SM = FALSE >
  - o leave\_SMB2: SMB2 = FALSE >
  - o enter\_SF: SF = TRUE >**END**

# Example – Factory Machine

Machine

- 1) A factory machine can be switched on and off.
- 2) When it is on it can then be started and becomes active.
- 3) When it is active it can run repeatedly until it is stopped.

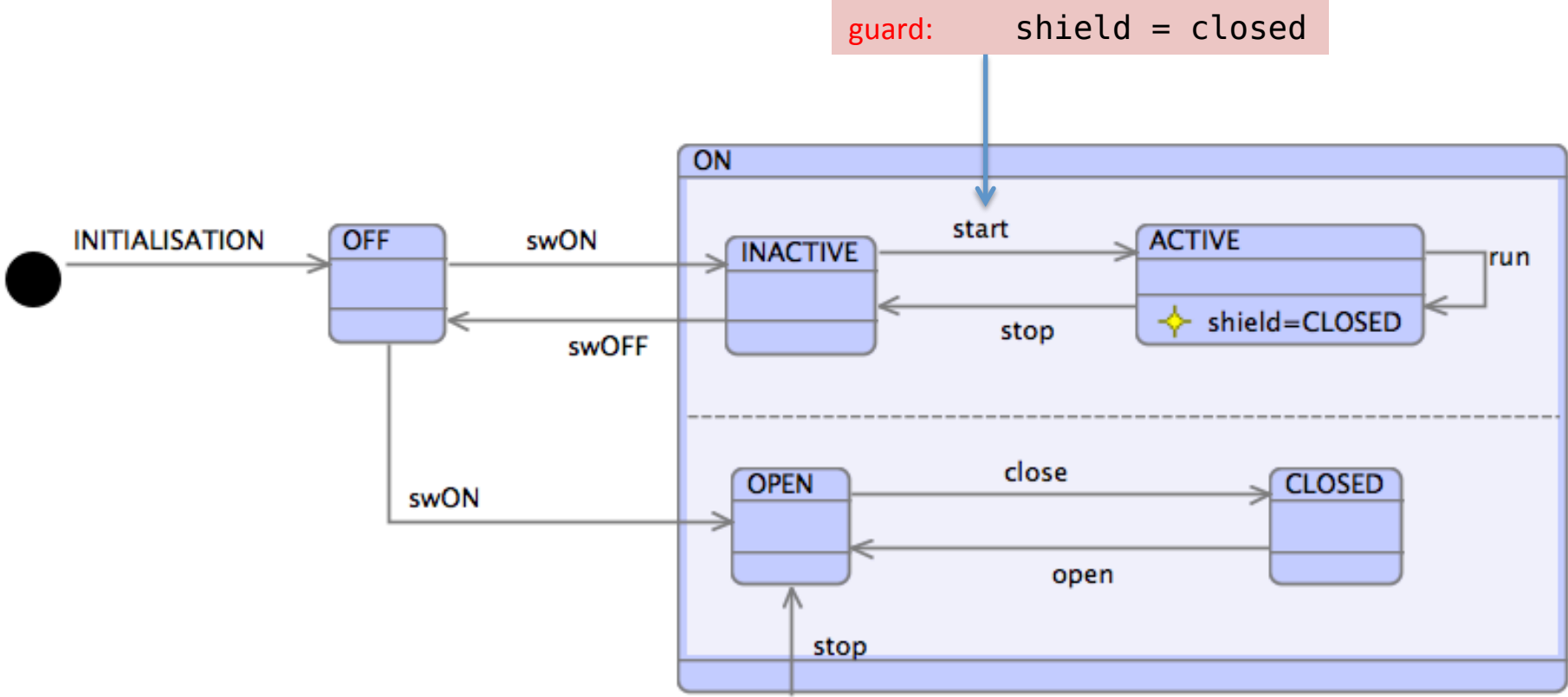
Shield

- 4) A separately controlled safety shield can be opened and closed when the machine is on.
- 5) The shield is opened automatically when the machine is stopped.

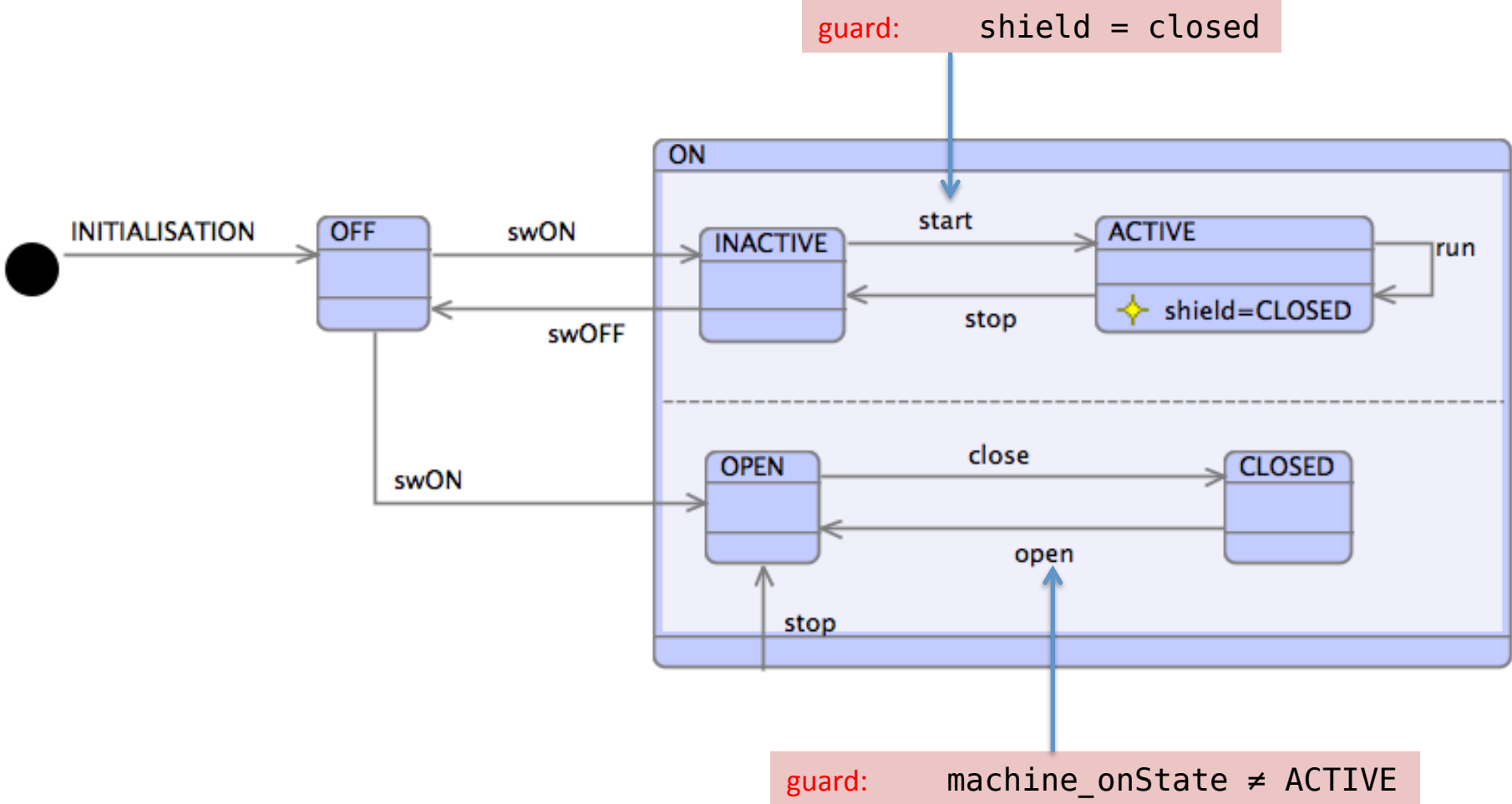
Invariant

- 6) Safety Requirement:  
The machine should never be in the active state (where runs can occur) with the shield in the open position.

# Example – Factory Machine



# Example – Factory Machine



`guard: machine_onState ≠ ACTIVE`

omitted for model checking demo on next page

# State-machine Animation showing invariant violation

ProB - platform:/resource/FactoryMachine/m0.machine.smd#\_Rr7yQK9qEeOjNJuF2Pfog - Rodin Platform - /Volumes/Data/RodinWorkspaces2.8/COMP3011

Lucida Grande 9

**Eve** | \*m0.machine.smd#0 | **State** | Ltl Count | Simulato | E "1

Checks | Event | Parameter(s)

- swON
- swOFF
- start
- stop
- run
- close
- open

```
graph LR
    Start(( )) -- INITIALISATION --> OFF[OFF]
    OFF -- swON --> INACTIVE[INACTIVE]
    INACTIVE -- swOFF --> OFF
    INACTIVE -- start --> ACTIVE[ACTIVE]
    ACTIVE -- stop --> INACTIVE
    ACTIVE -- run --> ACTIVE
    ACTIVE -- shield=CLOSED --> InvariantViolation[Invariant Violation]
    INACTIVE -- swON --> OPEN[OPEN]
    OPEN -- close --> CLOSED[CLOSED]
    CLOSED -- open --> OPEN
    OPEN -- stop --> STOP[ ]
    style STOP fill:none,stroke:none
```

**State**

Name

- ▼ m0
- machine
- machine\_onState
- ★ shield
- ▼ Formulas
- ▼ invariants
- ▶ machine\_onState ≠ machine\_onState\_NULL\_
- ▶ shield ≠ shield\_NULL ⇔ (machine = ON)
- ▼ ★ machine\_onState = ACTIVE ⇒ shield = C
- ▶ machine\_onState = ACTIVE
- ▶ ★ shield = CLOSED
- ▶ guards

**E "1**

m0

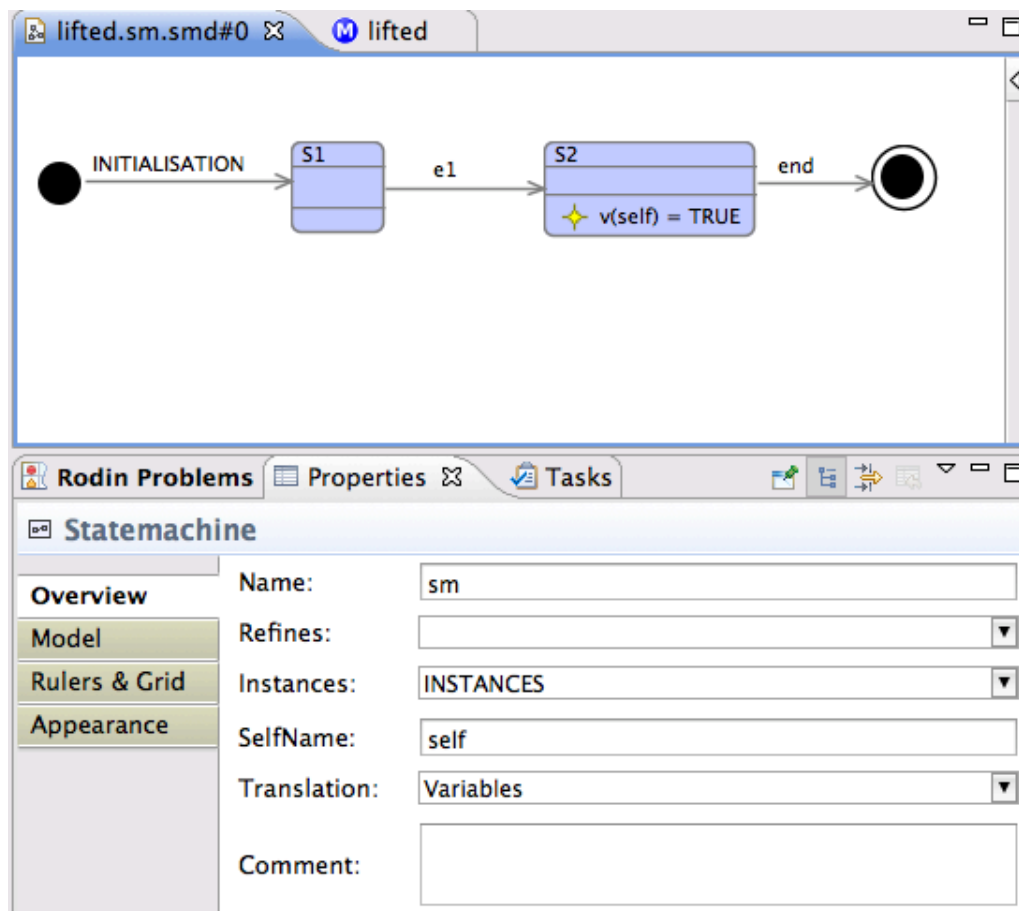
- open
- run
- start
- close
- swON
- INITIALISATION
- (uninitialised state)

**invariant violated!** **no event errors detected**



# Lifted (O-O) State-machines

- Statemachines can be ‘lifted’ to a set of instances in an O-O way
- Effectively, each instance has a “copy” of the statemachine
- Need to be able to define ‘self’ name in case of transition synchronisation



# Lifted (O-O) State-machines - Enumeration Translation

VARIABLES/INVARIANTS

$sm \in \text{INSTANCES} \rightarrow sm\_STATES$

SETS

$sm\_STATES = \{S1, S2\}$

EVENTS

INITIALISATION  $\triangleq$

$sm := \text{INSTANCES} \times \{S1\}$

$e1(self) \triangleq$

WHERE  $sm(self) = S1$

THEN  $sm(self) := S2$

END

# Lifted (O-O) State-machines - Variables Translation

## VARIABLES/INVARIANTS

```
S1   ⊆ (INSTANCES)
S2   ⊆ (INSTANCES)
partition((S1 ∪ S2), S1, S2)
```

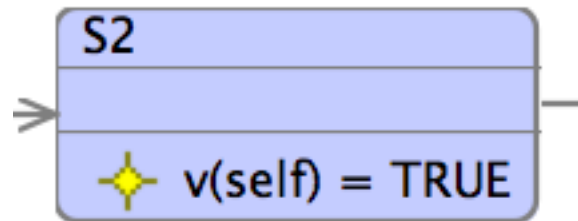
## EVENTS

```
INITIALISATION  $\triangleq$ 
    S1 := INSTANCES
    S2 := ∅

e1(self)  $\triangleq$ 
    WHERE self ∈ S1
    THEN  S1 := S1 \ {self}
         S2 := S2 ∪ {self}
    END
```

# Lifted (O-O) State-machines – Invariants (Variables Translation)

Something that must be true for the instance whenever an instance of the class is in that state.



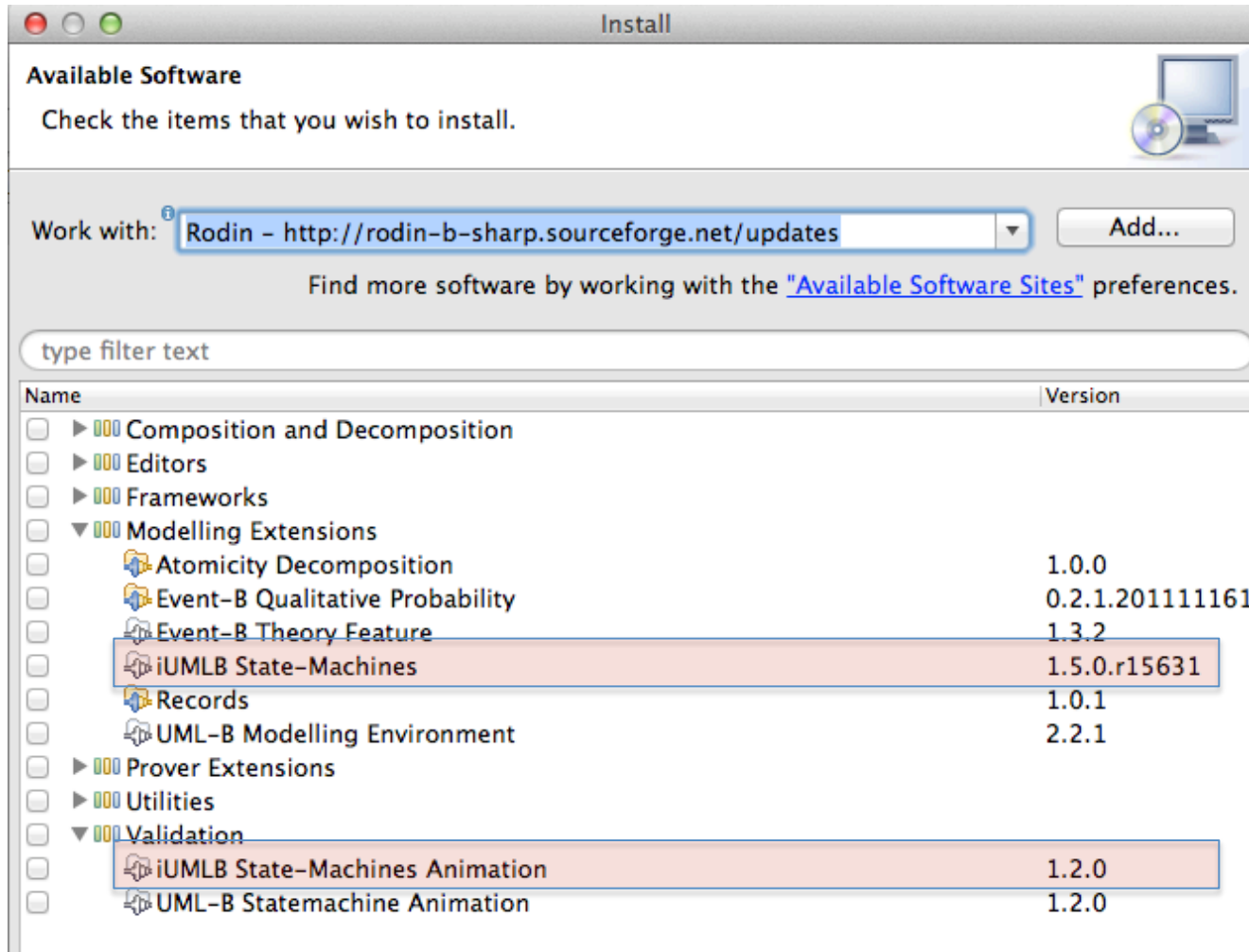
Translation:

$$\forall \text{self} \cdot (\text{sm}(\text{self}) = S2) \Rightarrow (\text{v}(\text{self}) = \text{TRUE})$$

# Installation

**IMPORTANT:** An extra update site has to be added to make some dependencies accessible. Use the **ADD** button below to add the following update site before installing iUML-B :-

<http://download.eclipse.org/modeling/gmp/gmf-tooling/updates/releases/>



# Summary

## Statemachines for modelling behaviour

- ▶ Nested statemachines in states
- ▶ Invariants in states
- ▶ Transitions elaborate events ...
- ▶ ... to control the sequence of event firing (a control flow)

## Choice of 2 translations

## Can be 'lifted' to instances

## Can be animated and model checked

- ▶ (front-end for Pro-B)