

Towards Modular Development in Event-B

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Event-B top-down development

- ▶ Refinement
- ▶ Decomposition

Pros and Cons

- ✓ Details can be introduced **gradually** into the formal model
- ✗ Large models with **monolithic structures**

- ▶ **Modularisation** (Iliasov et. al., 2010)
- ▶ **Feature composition** (Poppleton, 2008)
- ▶ **Parallel composition** (Silva and Butler, 2009)
- ▶ **Patterns** (Hoang et. al., 2009)
- ▶ **Generic instantiation** (Silva and Butler, 2009)

The presented proposal borrows many ideas from these approaches.

- ▶ Reuse models through **composition**.
 - ▶ Including **refinement-chain** of the sub-models.
- ▶ **Integrated smoothly** with the Event-B development process.
 - ▶ Accomodate changes **seamlessly**.

- ▶ Machine **A** includes machine **B**

machine **A**
includes **B**

- ▶ **A** inherits **B**'s **variables**
 - ▶ **A** inherits **B**'s **invariants**
 - ▶ **B**'s variables can only be modified via **event synchronisation**
- ▶ **Multiple instances** of **B** can be included via **prefixing**.

machine **A**
includes **p_B**

- ▶ Variables, events are **renamed** accordingly.

Machine Inclusion

Illustration

machine B

variables y

invariants

$J(y)$

events

event f

any u where

$G_B(y, u)$

then

$y := BAP_B(y, u, y')$

end

Machine Inclusion

Illustration

machine B

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invariants

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any u where

$G_B(y, u)$

then

$y := BAP_B(y, u, y')$

end

machine A

variables x

machine (flatten_)A

variables x

Machine Inclusion

Illustration

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variables x, p_y

Machine Inclusion

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machine B

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event f

any u where

$G_B(y, u)$

then

$y :| BAP_B(y, u, y')$

end

machine A
includes p_B

variables x
invariants

$I(x, p_y)$

machine (flatten_)A

variables x, p_y
invariants

$I(x, p_y)$

$J(y)$

machine B

variables y
invariants

$J(y)$

events

event f

any u where

$G_B(y, u)$

then

$y :| BAP_B(y, u, y')$

end

machine A

includes p_B

variables x
invariants

$I(x, p_y)$

events

event e

synchronises p_f

any t where

$G_A(x, t)$

$H_{AB}(x, p_y, t, p_u)$

then

$x :| BAP_A(x, t, x')$

end

machine (flatten_)A

variables x, p_y
invariants

$I(x, p_y)$

$J(y)$

machine B

variables y
invariants

$J(y)$

events

event f

any u where

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machine (flatten_)A

variables x, p_y
invariants

$I(x, p_y)$

$J(y)$

events

event e

any t, p_u where

$G_A(x, t)$

$H_{AB}(x, p_y, t, p_u)$

$G_B(p_y, p_u)$

then

$x : | BAP_A(x, t, x')$

$y : | BAP_B(p_y, p_u, p_y')$

end

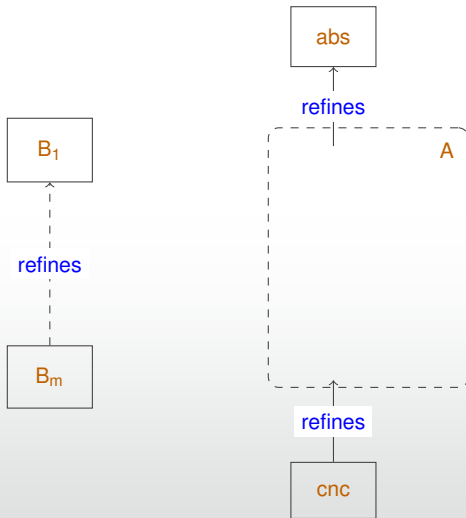
- ▶ Machine **A** includes refinement-chain $B_1 \longrightarrow B_m$.

machine **A**
includes $B_1 \longrightarrow B_m$

- ▶ **A** has **double interfaces**
 - ▶ To its abstract machine, **A** includes B_1
 - ▶ To its refinement, **A** includes B_m

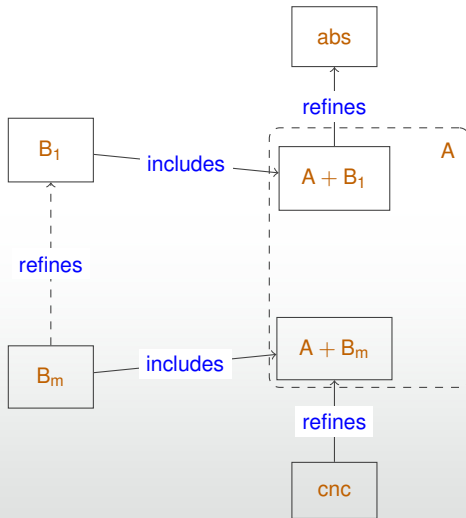
Refinement-Chain Inclusion

Illustration



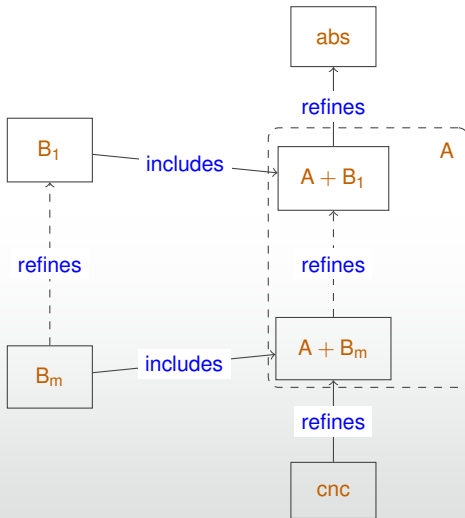
Refinement-Chain Inclusion

Illustration



Refinement-Chain Inclusion

Illustration



Refinement-Chain Inclusion

The Two “Interfaces”

machine $A + B_1$

events

event e

any t, u_1 where

$G_A(x, t)$

$H_{AB_1}(x, y_1, t, u_1)$

$G_{B_1}(y_1, u_1)$

then

$x :| BAP_A(x, t, x')$

$y_1 :| BAP_{B_1}(y_1, u_1, y')$

end

machine $A + B_m$

refines $A + B_1$

events

event e

any t, u_m where

$G_A(x, t)$

$H_{AB_m}(x, y_m, t, u_m)$

$G_{B_m}(y_m, u_m)$

then

$x :| BAP_A(x, t, x')$

$y_m :| BAP_{B_m}(y_m, u_m, y')$

end

The refinement is “almost” correct-by-construction.

Refinement-Chain Inclusion

The Two “Interfaces”

machine $A + B_1$

events

event e

any t, u_1 where

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machine $A + B_m$

refines $A + B_1$

events

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any t, u_m where

$G_A(x, t)$

then

$x :| BAP_A(x, t, x')$

end

then

$x :| BAP_A(x, t, x')$

end

The refinement is “almost” correct-by-construction.

- ▶ Guard-strengthening for G_A is trivial
- ▶ Action-strengthening for BAP_A is trivial

Refinement-Chain Inclusion

The Two “Interfaces”

machine $A + B_1$

events

event e

any t, u_1 where

$G_{B_1}(y_1, u_1)$

then

$y_1 : | BAP_{B_1}(y_1, u_1, y')$

end

machine $A + B_m$

refines $A + B_1$

events

event e

any t, u_m where

$G_{B_m}(y_m, u_m)$

then

$y_m : | BAP_{B_m}(y_m, u_m, y')$

end

The refinement is “almost” correct-by-construction.

- ▶ Guard-strengthening for G_{B_1} is guaranteed by B_m refines B_1
- ▶ Action-strengthening for BAP_{B_1} is guaranteed by B_m refines B_1

Refinement-Chain Inclusion

The Two “Interfaces”

machine $A + B_1$

events

event e

any t, u_1 where

$H_{AB_1}(x, y_1, t, u_1)$

then

end

machine $A + B_m$

refines $A + B_1$

events

event e

any t, u_m where

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end

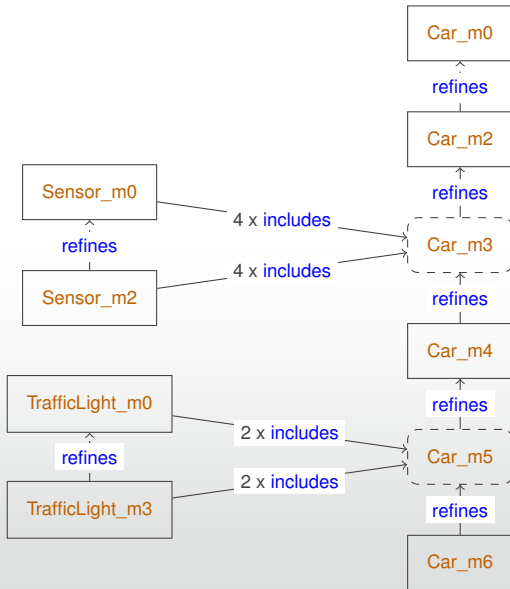
The refinement is “almost” correct-by-construction.

- ▶ Guard-strengthening for H_{AB_1} needs to be proved manually.

- ▶ We have applied the idea to several examples.
- ▶ Resulting in **hierarchical development**.
- ▶ Modelling effort is reduced.
- ▶ Proving effort is reduced.
- ▶ Easier to understand specification.

Example. Car on a Bridge

Development hierarchy



```
machine Car_m6
includes
  ML_out_Sensor_m2
  ML_in_Sensor_m2
  IL_out_Sensor_m2
  IL_in_Sensor_m2

  ML_TrafficLight_m3
  IL_TrafficLight_m3
```

```
(flatten_)ML_in
when
  ML_in_SNSR = TRUE
  ML_in_Snsr_01 = FALSE
  ML_in_ctrl_Snsr_01 = FALSE
  ML_in_DEP  $\neq$  IL_out_DEP
then
  ML_in_SNSR := FALSE
  ML_in_DEP := ML_in_DEP + 1
  ML_in_Snsr_10 := TRUE
end
```

```
event ML_in
synchronises ML_in_SNSR_off
when
  ML_in_DEP  $\neq$  IL_out_DEP
then
  SKIP
end
```

- ▶ Inclusion of **refinement-chain**
- ▶ **Syntactical**
- ▶ **Tool support** is needed.
- ▶ Reference machines/contexts from another project (see the next talk).